

## Algorithms and Uncertainty

Winter Term 2024/25

Tutorial Session - Week 11

### Exercise 1:

Show that the EXP3 algorithm can also be applied to an instance of Stochastic Multi-Armed Bandits from lecture 17.

Additionally, show that, when setting  $\eta = \sqrt{\frac{\ln n}{nT}}$  and  $\gamma = n\eta$ , this leads to an expected regret of at most  $3\sqrt{nT \ln n}$ .

**Hint:** You can use the bound on the external regret of EXP3 from lecture 20.

### Exercise 2:

Let each  $l_i^{(t)} \in \{0, 1\}$ . We consider the following Greedy algorithm. In each step  $t$ , the algorithm selects  $I_t$  which satisfies  $I_t = \arg \min_{i \in [n]} L_i^{(t-1)}$ , i.e. the expert with the best cumulative cost so far (ties are broken adversarially).

Show that  $L_{\text{Alg}}^{(T)} \leq n \cdot \min_i L_i^{(T)} + (n - 1)$